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Use of significance test logic by scientists in a novel reasoning task

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Although statistical significance testing is one of the most widely-used techniques across science, previous research has suggested that scientists have a poor understanding of how it works. If scientists misunderstand one of their primary inferential tools the implications are dramatic: potentially unchecked, unjustified conclusions and wasted resources. Scientists' apparent difficulties with significance testing have led to calls for its abandonment or increased reliance on alternative tools, which would represent a substantial, untested, shift in scientific practice. However, if scientists' understanding of significance testing is truly as poor as thought, one could argue such drastic action is required. We present evidence using a novel reasoning task that scientists may understand the logic of significance testing better than previously thought. Scientists may not be as statistically-challenged as often believed; reforms should take this into account.

2 For most of the past century, the dominant method of statistical inference has been statistical
3 significance testing (SST). In a significance test, the statistical evidence in the form of a test statistic
4 is compared to what would be expected under a particular hypothesis (often called the “null”
5 hypothesis). If it would be surprising to observe evidence as strong as what was observed under
6 this hypothesis, the evidence is deemed strong enough to call the assumed hypothesis into doubt,
7 at least tentatively [see also 1,2]. The rarity of evidence as strong as what was observed under the
8 assumed hypothesis—the so-called p value—is the typical way that results of significance tests
9 are reported. The key feature of SST for our purposes is the assessment of evidence by means of
10 comparing a result to a “null” distribution.

11 Despite the use of SST in a majority of research projects across fields, there is debate over
12 whether scientists understand SST and can use it competently. Methodologists and statistical
13 cognition researchers point to evidence from questionnaires and vignette studies to argue that
14 researchers do not, in fact, grasp the core logic of SST. In one highly influential study of research
15 psychologists, Oakes [3] presented six statements about a hypothetical significance test result to
16 be categorized as true or false (e.g., “[The p value provides] the probability of the null hypothesis
17 being true”). Despite all of these statements being false, 97% of the research psychologists
18 categorized at least one as true. Oakes argues that this shows that the participants have an
19 “[un]sound understanding of the logic of the significance test” (p. 82).

20 Oakes’ basic method and results have been replicated and extended with various groups,
21 showing that students [4], instructors [5], and statisticians [6] all misinterpret SST results.
22 Moreover, these misinterpretations are difficult to eliminate even through targeted interventions
23 [7]. As a result, many have argued that use of SST should be discontinued or dramatically
24 reduced, and may even contribute to wide-spread replication problems in the sciences [3,8–11].

25 The interpretation of studies of researchers’ understanding of SST is limited, however, by their
26 methodology. A typical study presents a vignette describing research results. Statistical results
27 are offered to the participants (e.g., a t statistic and p value), who are then asked to explicitly
28 give or endorse various interpretations. These responses are taken to represent participants’
29 understanding, or misunderstanding, of SST. However, there are reasons to be cautious of
30 drawing strong conclusions from these studies, including the abstract nature of such vignettes,
31 the lack of investment researchers have in the fictional research, and their disconnection from
32 research activity (e.g., experimentation and replication). It is unclear how well vignette studies
33 (including ones by the present authors: [12,13]) tap understanding of the core logic of SST rather
34 than, say, familiarity with the technical terminology used to present statistical results. Conceptual
35 understanding and fluency with common representations are both important, but are distinct.

36 A second major piece of evidence for misunderstandings of SST logic is reasoning errors in
37 published papers [14–17]. Like evidence from vignette studies, however, these errors are difficult
38 to interpret as misunderstandings of SST logic *per se*. These examples show that whatever process
39 lead to the statistical conclusion was flawed in some way, but many processes contribute to such
40 conclusions. Cognitive [e.g., 18], technological [e.g., 19], and social processes [e.g., 20] have all
41 been assigned some blame for statistical reasoning failures.

42 In deciding how to improve statistical reasoning, it is crucial to know where the problems lie.
43 The *fact* of reasoning problems tells us little about their *source*. In assessing potential interventions,
44 however, the source is crucial. Some interventions might focus on the social aspects (e.g.,
45 decreasing the need for “significant” results for prestige), some on technological aspects (e.g.,
46 presenting statistical results in ways that were previously impossible), and some on cognitive
47 aspects (e.g., adopting Bayesian procedures because these are claimed to be better understood).

48 To avoid conflating basic reasoning failures and lack of fluency with common statistical
49 terminology, we avoid using common statistics—or, indeed, any numbers—at all. Instead of
50 focusing on familiar statistical language and tests participants’ fluency with existing procedures,
51 we adopt a different approach: we test working scientists’ understanding of the basic conceptual
52 framework underlying SST using a simulated experimental task.

The key innovation allowing us to focus on SST reasoning was to design an experiment that prevents the use of alternative strategies. A critical feature of SST is that the use of a null distribution destroys information about effect sizes and sample size. In fact, this aspect of SST reasoning is often criticized, while alternative methodologies focus on effect sizes (point estimates, confidence intervals, equivalence, likelihood, Bayesian priors/posteriors). We offered our participants only the information in a p value, and participants had to understand or discover how to obtain that information. Their task was to use this information to come to a decision about the true sign of an effect through repeated experimentation.

If participants have poor understanding of SST, they would 1) often come to the wrong conclusion, in spite of ample information; 2) show error rates that are only weakly associated with true effect size; 3) be unable to articulate strategies for performing our task; 4) be sensitive to misleading, task-irrelevant information; 5) be insensitive to SST-relevant information. The scientists in our sample often came to the right conclusion, and their performance showing sensitivity to the SST-relevant information they were given. Moreover, they explicitly reported using SST strategies. Our results suggest that common methods for assessing scientists' competence may miss important aspects of their statistical knowledge, and hence that the case for abandoning significance testing may be overstated.

1. Testing reasoning by withholding information

In tests of perception, it is common to eliminate one cue in order to assess the ability to use another: e.g., eliminating brightness cues to test colorblindness [21]. If color is the only useful cue for reading a number on a card, deficits in color vision make the number difficult to read. We adopt a similar strategy to test statistical reasoning: we eliminate numerical information from statistical results to test scientists' ability to interpret results with reference to a null sampling distribution, a central element of SST logic. Without numerical information, many other strategies and heuristics, such as confidence intervals, or Bayesian inference, are difficult or impossible to apply.¹

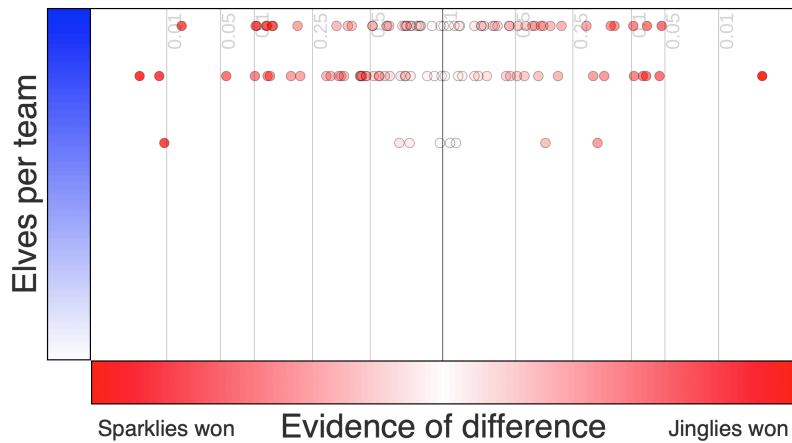
Participants were scientists or trainees recruited via social media. Our statistical reasoning task required them to perform a series of experiments to judge which of two groups of "Christmas elves" — "Jinglies" or "Sparklies" — could make more of a particular toy. A demonstration version of the task can be found at https://richarddmoney.github.io/Morey_Hoekstra_StatCognition/articles/task_demo.html. Because the study was run around the Christmas holiday season, we hoped the theme would make the task more engaging. The numerical information for an experiment, including sample size and the test statistic, was translated into color and location and displayed as a point on a two-dimensional visual interface (Figure 1). Participants could change the sample size per group for each experiment (increasing the time required to return a result), but did not know its numerical value. Importantly, the meaning of the colors and locations was unknown to the participants, aside from the monotone relationship with the sample size and statistical evidence.

Participants were randomly assigned to one of 15 effect size conditions: either no difference ($\delta = 0$), or $\delta = \pm 0.1, \pm 0.185, \pm 0.296, \pm 0.433, \pm 0.596, \pm 0.785$, or ± 1 standard deviation units. Each participant had a 25% probability of being assigned $\delta = 0$, with the other 75% being randomly and uniformly distributed across the remaining 14 effect size conditions. These true effect sizes were not revealed to the participants. Their goal was to determine the sign of the effect (i.e., which of the two teams is truly faster).

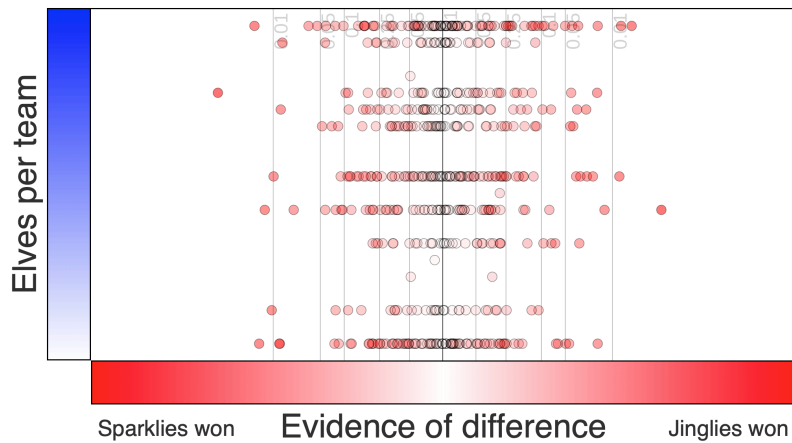
Consistent with the fictional two-sample design, statistical evidence for each "experiment" was sampled from a normal distribution with mean that depended on the (chosen, but unknown) sample size and their randomly assigned effect size:

$$Z \sim \text{Normal}(\delta\sqrt{n/2}, 1)$$

¹A formal statistical explanation showing that the task is difficult or impossible to perform using non-SST logic is given in Section 3 of [Supplement A](#).



(A) Random shuffle reports by one participant in the "wide" condition.



(B) Random shuffle reports by one participant in the "narrow" condition.

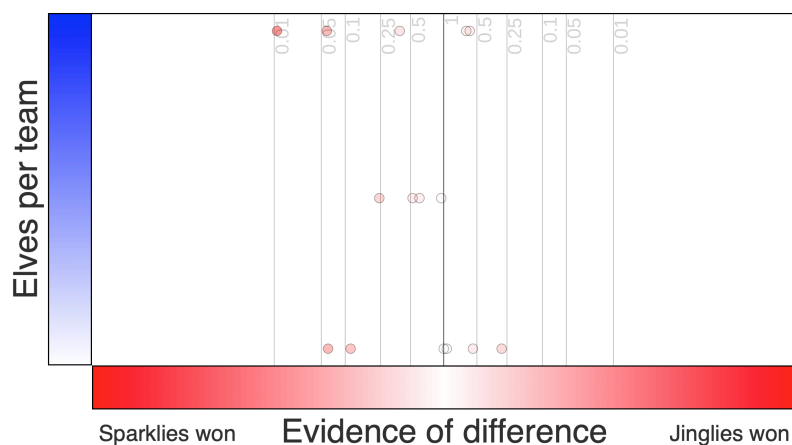
(C) Experimental samples by the same participant as shown in (B). This participant responded that the two groups were the same; the true effect size was -0.1 , so their response was a false negative.

Figure 1: Examples of the experimental interface with several participants' samples. The x -axis monotonically (but nonlinearly) related to the strength of the statistical evidence (z statistic) favoring one group; the y -axis is monotonically (but nonlinearly) related to the sample size. Underlying numerical values of the statistical evidence and sample sizes were unknown to the participant. Corresponding p values and vertical lines are given for reference; they were not shown to the participants.

99 The Z test statistic was mapped into a horizontal location on the interface through an arbitrary
100 function unknown to the participant. Participants were randomly assigned to one of two mapping
101 functions: a “wide” function, and a narrow function (see Supplement A, section 1.2 for full
102 mathematical details). Figures 1A and B show the visual effect of this manipulation. Statistically,
103 these two conditions were identical; visually, they were not.

104 This visual manipulation was crucial to study, because it allows assessment of participants’ use
105 of the null sampling distributions. In addition to being able to sample fictional “experiments”,
106 participants could sample “random shuffle reports” that were described as the results of
107 experiments with random assignment of elves to groups: that is, the result of experiments in
108 which the null hypothesis was true. These results took no time to return. Participants were not
109 told how to use these samples, only that they might use them.

110 Our experiment was constructed such that the only way to assess the evidence in the data
111 was by comparison of the fictional experimental results to a null sampling distribution: either
112 the one provided by the random shuffle reports, or a simpler null that assumes that the evidence
113 will favor one team or the other with 50% probability. Thus, the information afforded only the
114 information in a p value, but it was not described as such; participants had to discover for
115 themselves how to use the information.

116 After sampling as many “experiments” and “random shuffle reports” as they liked,
117 participants could report whether they believed Jingles or Sparklies were the better team, that
118 they could not detect a difference, that there was no difference, or that they were bored and
119 wanted to stop. Following their decision they were asked several open-ended questions about
120 their strategy, along with some opinion and demographic questions. Our central questions are
121 whether participants can effectively find the “truth”, whether they report strategies consistent
122 with SST, and whether their behaviour shows evidence of strategic SST use.

123 Here, we report the results of 506 scientists or trainees who completed the statistical reasoning
124 task.

125 2. Participant sampling behavior

126 Participants sought out information that would be necessary for significance tests. They made
127 heavy use of shuffle reports (Figure A2). Across all true effect sizes, participants sampled a median
128 of 152 shuffle reports (range: 1-2034; in both panels A and B, lines show robust regression fits [22]).

129 Participants also made use of “replications” of the fictional experiments. Figure 2B shows the
130 distribution of the number of experiments sampled as a function of the true effect size. Median
131 numbers of experiments range from 20 when Jingles and Sparklies were equally fast, down to 9
132 when the true effect size was $\delta = 1$ and thus the effect was relatively easy to detect ($Kruskal -$
133 $Wallis\chi^2(7) = 45.70, p < .001$). When the effect size is small and difficult to detect, participants
134 experimented more before deciding.

135 3. Success rates identifying effect sign

136 Decision rates as a function of true effect size are shown in Figure 3.

137 Of the 136 participants for whom the null hypothesis was true (i.e. $\delta = 0$), 20 participants
138 (14.7%) incorrectly indicated an effect. This is larger than the typically-accepted 5% false positive
139 rate in many sciences; however, participants were performing a novel task with no recourse
140 to numbers or statistical software. Those who did not indicate an effect when $\delta = 0$ tended to
141 indicate that they *did not detect* an effect (103; 75.7%), which is the correct conclusion from the
142 SST perspective. The other 13 (9.6%) indicated that the groups were the same, which under SST
143 is typically considered a fallacy.

144 When there was a true effect ($\delta \neq 0$), correct decisions increased as a function of effect size,
145 plateauing at about 95%. Of the 370 participants for whom $\delta \neq 0$, only 2 (0.5%) indicated the
146 incorrect team [a sign, or Type S, error; 23]. For larger effect sizes, participants never incorrectly
147 indicated that the two groups were the same.

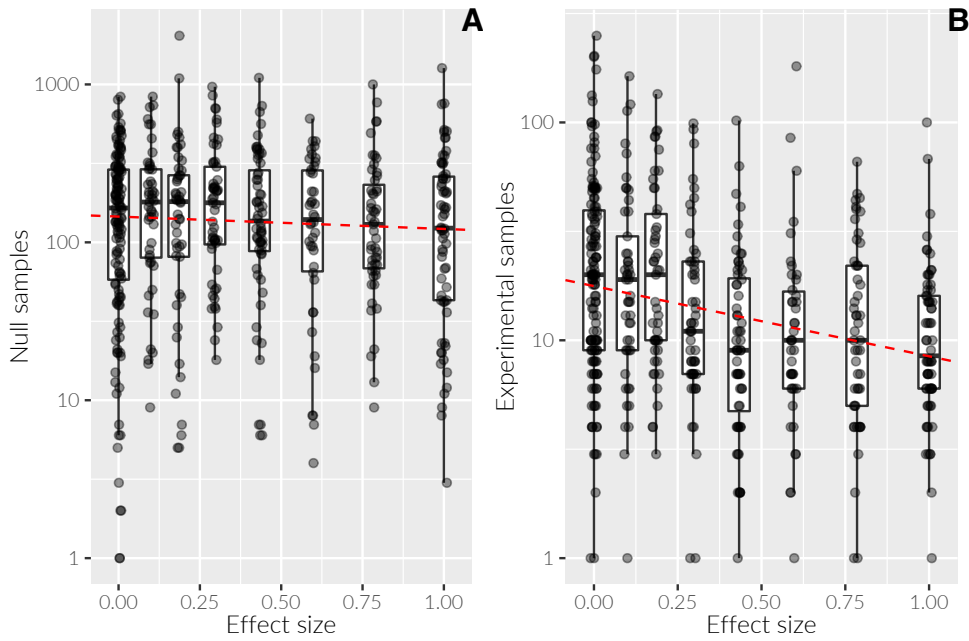


Figure 2: Sampling behavior by effect size. Each point represents a participant. A: Number of samples from the null distribution as a function of true effect size. B: Number of samples of fictional ‘experiments’ as a function of true effect size. Note that the y axis is logarithmically scaled. Lines are robust regression fits. Positive and negative effect sizes have been collapsed.

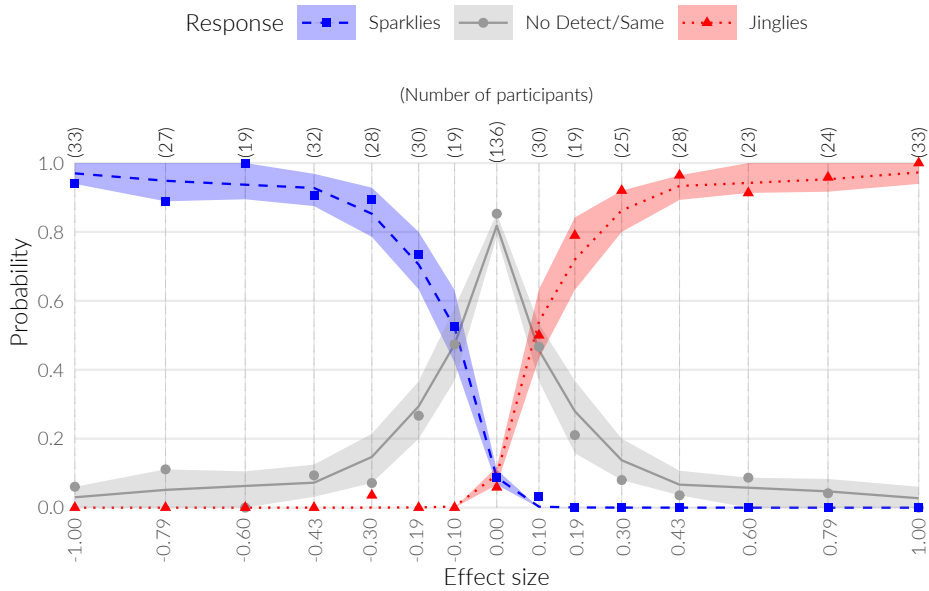


Figure 3: Observed and fitted probabilities for each effect size and response. For negative and positive effect sizes, the correct response "Sparklies" or "Jingles" respectively. Fitted probabilities are from the signal detection model outlined in Supplement A. Lines show predicted probabilities; ribbons show where 68% of the observed probabilities should fall given the predicted probabilities. These limits are approximate due to the discreteness of the response.

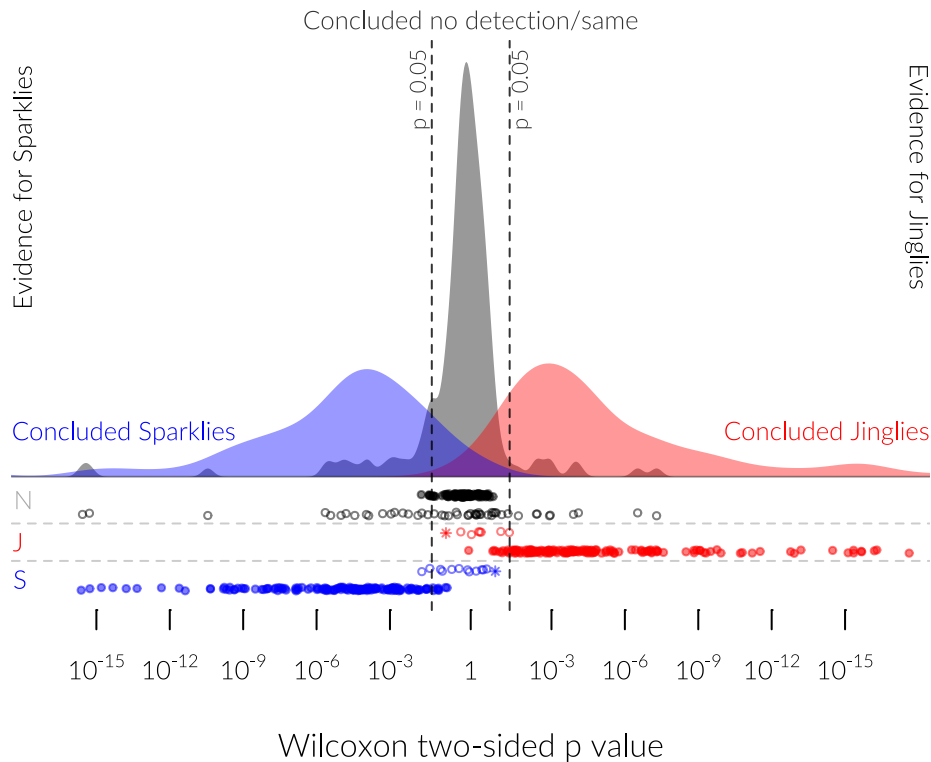


Figure 4: Statistical evidence underlying participants' decisions. The Wilcoxon p value (x axis) used as a rough index of evidential strength in the display. Kernel density estimates for the evidence are shown for three relevant conclusions. Each point at the bottom represents a single participant. Filled circles show correct decisions; hollow circles, incorrect decisions. The two asterisks show sign errors.

148 Signal detection theory gives us another perspective on the decision rate shown in Figure 3,
 149 allowing us to correct for the baseline of errors that occur in the null condition [24]. We combine
 150 the “false alarm” rate when $\delta = 0$ (14.7%) with the “hit rates” for all other conditions using a
 151 simple signal detection model; see Supplement A, section 8 for model details. The fitted model
 152 yields d' parameters that range from 1.41 when $\delta = 0.1$ to 3.24 when $\delta = 1$.

153 4. Use of information in the display

154 Another way of evaluating participants' responses is whether they reflect the information in the
 155 display at the time the decision is made, taking into account all points. To roughly quantify the
 156 evidence for a difference for each participant, we computed two p values from Wilcoxon tests
 157 using the fictitious experimental results as they stood when the participant made their decision:
 158 a signed-rank test on the experimental samples alone, and a rank-sum test between the shuffle
 159 reports and the experimental samples. These two p values indicate the information available
 160 to participants using sign-like significance tests and those using the null samples, respectively.
 161 The rank-sum p value is based on more information and so was typically lower. It makes little
 162 difference to the qualitative results, but to fairly account for the information available to the
 163 participant, we used the smaller of the two p values. In general, smaller p values suggest a larger
 164 observed between the shuffle reports and the experiments, allowing us to compare the stimulus
 165 the participants were given to their decisions.

166 Figure 4 shows the distribution of Wilcoxon p values (arranged by the direction of the
167 decision). Kernel density estimates show the distributions of p values when participants
168 indicated that Sparklies were faster, no detection/same, or that Jinglyes were faster. With a few
169 notable exceptions, participants' conclusions appear reasonable given the information in the
170 display, though a few participants appear to ignore clear evidence of an effect. We provide an
171 interactive app for exploring participants' individual responses at [https://richarddmorey.
172 shinyapps.io/explore/](https://richarddmorey.shinyapps.io/explore/).

173 5. Sensitivity to SST-Relevant Information

174 In addition to a random effect size, participants were also randomly assigned to one of two
175 transformations of the location/color test statistic from an underlying z statistic. Of particular
176 interest was how the transformation affected responding for the same visual deviation from the
177 center.

178 The visual effects of the manipulation are shown in Figure 1, panels A and B. The two
179 experimental conditions used different arbitrary monotone mappings from the underlying Z -
180 statistic to the visual space. Intuitively, this would be like deciding to use Z^3 instead of Z in
181 all Z tests; one would need to adjust the significance criteria to account for the cubing (e.g., use
182 $|1.96^3| = 7.53$ instead of $|1.96|$ for a $\alpha = 0.05$ level test), but the underlying test remains the same.
183 The manipulation changes only the visual impression of the sampling distributions, allowing us
184 to see how sensitive their responses are to the null sampling distribution as represented by the
185 random shuffle reports.

186 If participants were using the shuffle reports to interpret the data, as would be predicted if they
187 were using SST logic, the transformation should affect their interpretation of the visual evidence:
188 a visually-extreme point should be more discounted against the sampling distribution that is
189 wider. When we break down responses by the *visual* extremeness of the evidence, responses in
190 two conditions should appear different; when we break down responses by *statistical* extremeness
191 (i.e., the p value) responses in the two conditions should appear very similar, because the visual
192 manipulation is irrelevant given the p value.

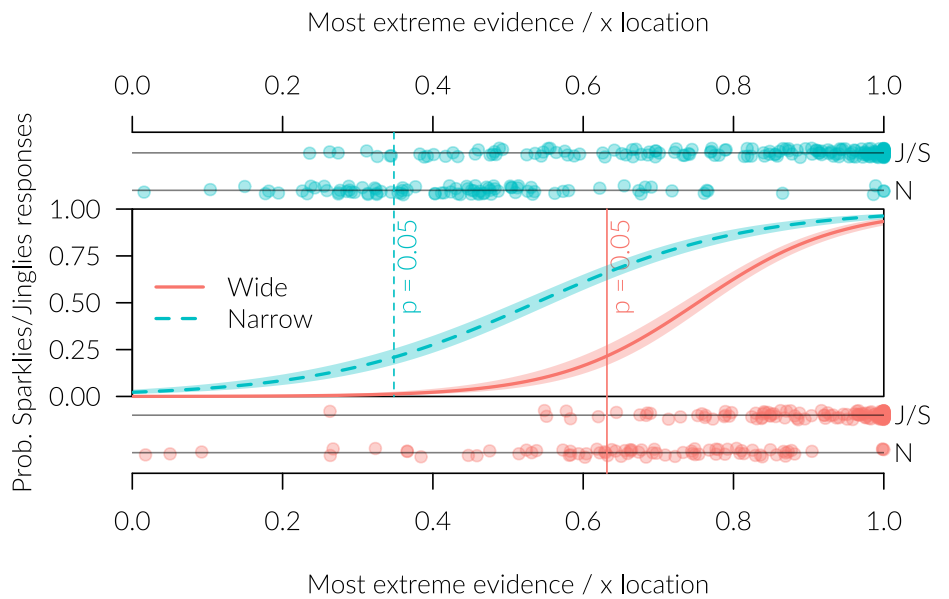
193 Figure 5 (top) shows responses (no detect/same or Jinglyes/Sparklies) as a function of the
194 most extreme experiment sampled (x axis) and the transformation. There was a strong effect of
195 the transformation consistent with use of the null sampling distribution; participants randomly
196 assigned to the "narrow" evidence transformation responded "Jinglyes/Sparklies" for much less
197 visually extreme evidence (sequential LRT: $\chi_2^2 = 35.492, p < .001$).

198 A logistic regression relating responses to the visual extremeness of the evidence and the
199 transformation provides predicted probabilities of responding "Jinglyes/Sparklies" when the
200 visual evidence corresponded to $p = 0.05$ for the null sampling distribution. In both the wide
201 and the narrow conditions, the predicted probability of a "Jinglyes/Sparklies" response at the
202 critical value was about 22%, despite that in the wide transformation condition this point was
203 about twice as visually extreme.

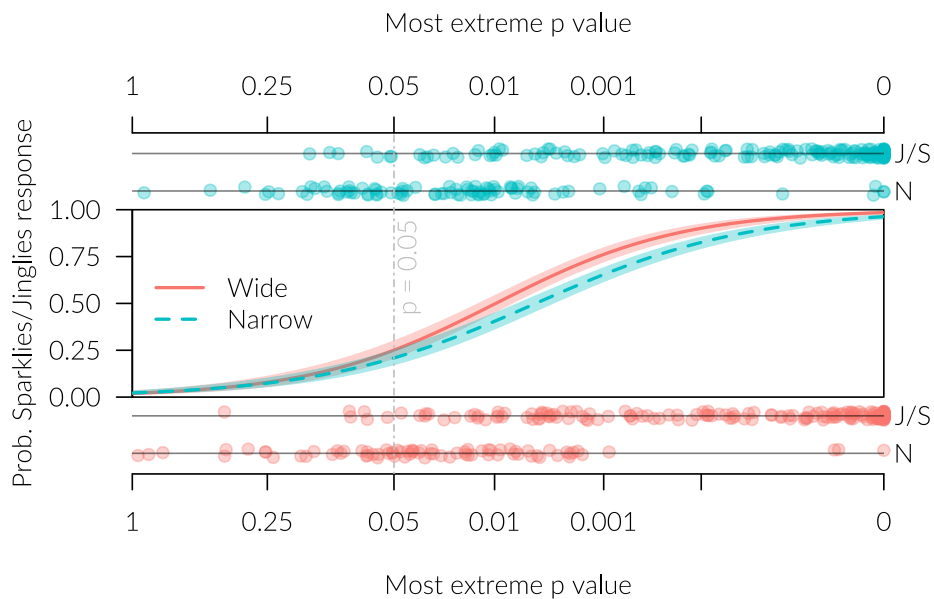
204 Applying the same analysis to the responses corrected for their respective sampling
205 distributions (Figure 5, bottom) almost completely eliminates the effect of experimental condition,
206 as would be expected if most participants were using the sampling distributions to calibrate
207 (sequential LRT: $\chi_2^2 = 3.505, p = 0.173$). It is noteworthy that when the responses are aligned by
208 sampling distribution, the wide condition appears to slightly dominate; this is consistent with
209 some participants incorrectly using the non-diagnostic visual extremeness to perform the task. If
210 more people had been fooled by the irrelevant width of the null sampling distribution, we would
211 expect this effect to be substantially larger.

212 6. Self-Reported SST Strategies

213 After they reported their decision regarding which team they believed was faster, we asked
214 participants three questions about how they performed the task: what was the most salient



(A) Predicted response probabilities relative to visual extremity. Vertical lines show the critical 0.05 for the corresponding null sampling distribution.



(B) Predicted response probabilities relative to the null sampling distributions (implicit p values).

Figure 5: The effect of the evidence transformation manipulation on responding. Points on top (narrow scale; $q = 7$) and bottom (wide scale; $q = 3$) represent participants' decisions as a function of the most extreme experiment sampled. See the methods details for the interpretation of q . "N" indicates a "no detect" or "same" response; "J/S" indicates a response in favor of a difference between the groups. Curves show predicted probability by a logistic regression fit with standard errors.

Table 1: Frequencies of self-reported strategies.

	Strong	Only weak	Neither	Total	No shuffles	Missing
Count	362	69	75	506	28	29
%	71.54%	13.64%	14.82%	100%	5.53%	5.73%

215 information for their decision, what was their general strategy, and whether/how they used the
216 shuffle reports.

217 We coded their responses according to whether they indicated comparing to the shuffle
218 reports or using them to assess sampling variability (which we term “strong” significance
219 testing strategies), assessing asymmetry in the display (a “weak” significance testing strategy,
220 because it ignores information), and whether they explicitly deny using the shuffle reports (see
221 Supplement A, section 7 for coding details).

222 As Table 1 shows, a large majority of participants (362, 71.54%) indicated using strong
223 significance testing strategies. We should be cautious in directly interpreting this high number
224 alone, however, because participants were told in the instructions that the shuffle reports could be
225 used for assessing sampling variability. We did this to make clear what the shuffle reports were,
226 but without explaining *how* to use them. To some extent, then, the text responses may reflect
227 the instructions. However, the data strongly suggest a deeper understanding; first, among the
228 responses were richer, lucid descriptions of SST logic, such as:

229 “[t]he random [shuffles] showed quite often such ‘strong evidence’, even at high sample
230 sizes. That should not happen when the evidence is really strong, so probably the end of
231 the scale was not [so] strong evidence. . . The random [shuffles] helped me to judge how
232 common misleading evidence in that order of magnitude is, and after 5 samples from the
233 real experiment I concluded that this result is probably not misleading evidence.”

234 Secondly—and most importantly—the instructions did not tell the participants how they
235 should use the shuffles reports, yet many participants gave detailed accounts. Combined with
236 the other reported results, this strongly suggests that our participants—with some exceptions—do
237 understand the basic SST logic and can deploy it to correctly solve novel problems.

238 7. Discussion

239 Although it has previously been suggested that scientists have dramatic misunderstandings of
240 SST logic, scientists and trainees in our experiment demonstrate both understanding and the
241 ability to use the logic to come to the correct conclusion in a simulated statistical task. Moreover,
242 they report strategies consistent with SST, and signatures of SST reasoning can be seen in their
243 responses. Because we removed numerical effect size and sample size information — making
244 strategies other than pure significance testing difficult or impossible to apply — our results
245 are evidence that scientists *can* successfully deploy SST logic. It is still an open question what
246 causes typical SST reports to be misunderstood so often, but we have not found evidence that the
247 problem is misapprehension of its underlying logic.

248 Our findings echo other demonstrations that human reasoning can, under some conditions, be
249 better than previously understood. [25,26]. Suggestions that SST be discontinued due to scientists’
250 apparent misunderstandings may be hasty. Of course, there may be other reasons to abandon
251 SST, but our work shows that given the opportunity, scientists successfully deploy basic SST
252 logic. In spite of scientists’ real-life statistical behaviour often resembling a “ritual” [27], when
253 we eliminate the ritual — no p value, or any other familiar number, was offered — they think
254 statistically, very often arriving at the correct conclusion about the sign of the effect.

255 We wish to emphasize what we cannot, and do not, argue. First, we cannot argue that simply
 256 because scientists can successfully use SST logic, that they *do* in real situations, or that specific
 257 instantiations of SST, such as p values, are used well. We specifically set out to abstract the logic
 258 away from the typical situations in which scientists use the logic. This has the benefit of being
 259 helping to identify where problems might be, but the downside that generalizing the results
 260 will require further work. We also cannot address other potential arguments against SST, such
 261 as philosophical ones.

262 Finally, we hope to provide a fresh method and perspective on a long-standing debate in
 263 statistical cognition. Simulation-based approaches to teaching statistics have long been touted [28,
 264 29]. Simulation-based approaches to *studying* scientists' statistical reasoning may also be profitable,
 265 particularly in studying reasoning that is difficult for participants to articulate formally. If we are
 266 to reform statistical education and practice in the sciences, we should base that reform on diverse
 267 lines of evidence about scientists' reasoning. Understanding and harnessing scientists' already-
 268 existing competence in statistical reasoning is essential to developing effective methodological
 269 reforms.

270 8. Methods

271 (a) Participants

272 Participants were recruited via social media platforms such as Twitter and Facebook. All
 273 participants gave informed consent. Data inclusion criteria included sampling at least one shuffle
 274 report and experimental result, working in a scientific field, having at least some University
 275 education in science, and that it was their first time participating. Details are given in [Supplement](#)
 276 [B](#).

277 After applying all inclusion criteria, 506 participants remained for analysis.

278 (b) Experimental Design and Procedure

279 Each participant was randomly assigned to one of eight true effect sizes (from $\delta = 0$ to $\delta = 1$)
 280 and one of two evidence powers ("wide" $q = 3$ or "narrow" $q = 7$; see "Evidence Distributions"
 281 below). The probability of being assigned $\delta = 0$ was 25%, while the remaining effect sizes were
 282 equally probable at 11%. The probability of assignment to either evidence power was 50%. Details
 283 are given in Table 1.1 in [Supplement A](#).

284 After offering informed consent, participants read the cover story and instructions. During
 285 the instructions, the participant was introduced to the task through sampling random shuffle
 286 reports. After a brief recap of the instructions, participants performed the main task — sampling
 287 either random shuffles or experiments — until they made a decision about which, if either, elf
 288 group was faster. They were then asked several open-ended questions about their strategy, some
 289 informational questions (results in [Supplement B](#)) and debriefed.

290 Qualtrics' duration estimate indicated that the median time spent on the experiment was 21
 291 minutes.

292 (c) Evidence distributions

293 The evidence/horizontal (x) location test statistic presented to the participant was derived from
 294 a transformed Z statistic:

$$Z \sim \text{Normal}(\delta \sqrt{n/2}, 1)$$

295 where δ is a true effect size (randomly assigned to each participant, from 0 to 1) and n is the
 296 selected but unknown sample size (from 10 to 200 participants per group). Z then transformed to

297 the (-1,1) space:

$$x = \text{sgn}(Z) \left[1 - \left(1 - F_{\chi_1^2} \left(Z^2 \right) \right)^{\frac{1}{q}} \right], \quad -1 \leq x \leq 1.$$

298 where $F_{\chi_1^2}$ is the cumulative distribution function of a χ_1^2 random variable, and $q \in \{3, 7\}$ was
 299 randomly assigned for each participant. $x = -1$ represented the left edge of the interface, $x = 0$
 300 the middle, and $x = 1$ the right edge. The setting of q determined how spread out the test statistic
 301 was on the display. This arbitrary transformation was done to ensure that the test statistic's
 302 distribution was unfamiliar to the participant. See [Supplement A](#) for more details, including
 303 graphical depictions of the evidence distributions.

304 (d) Coding of open-ended strategy questions

305 We determined the coding scheme and independently categorized the first 20 participant,
 306 discussing the source of disagreements. After categorizing the remaining participants, some
 307 disagreements were resolved through mutual agreement, and a discussion between the authors
 308 was had over what caused the disagreements. The remainder of the disagreements were re-coded
 309 separately, and a final round of discussion resolved the remaining disagreements. The coding of
 310 participants' responses is described in detail in [Supplement B](#).

- 311 • **Funding:** This research was not supported by external funding.
- 312 • Compiled 2020-11-04 16:45:34 (Europe/London) under R version 4.0.3 (2020-10-10).

313 **Ethics.** This research project was evaluated by the Cardiff University School of Psychology (application
 314 number EC.18.12.11.5526G). It was found to be within the ethical guidelines for experiments with human
 315 participants. All participants gave informed consent prior to their participation.

316 **Data Accessibility.** Data and relevant code for this research work are stored in GitHub: https://github.com/richardmorey/Morey_Hoekstra_StatCognition and have been archived within the Zenodo
 317 repository: <https://doi.org/10.5281/zenodo.3877106>
 318

319 **Authors' Contributions.** RDM conceptualized and designed the study in consultation with RH. RDM
 320 analysed the data and created the materials and figures. The manuscript was written by RDM and RH.

321 **Competing Interests.** The authors declare no conflicts of interest.

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